

Integration Exercises

A. Compute the following definite integrals using basic geometry.

1. $\int_{-4}^{10} 6x + 4 \, dx$ 2. $\int_1^6 2 + \sqrt{6x - x^2} \, dx$ 3. $\int_{-2}^4 |x| \, dx$

B. Compute the following definite integrals using Reimann Sums.

1. $\int_{-4}^{10} 6x + 4 \, dx$ 2. $\int_0^3 x^2 + 3x - 4 \, dx$ 3. $\int_{-1}^7 \pi \, dx$

C. Express the following limits as definite integrals, and then compute them.

1. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \left(2 + \frac{3i}{n}\right)^2 \frac{6}{n}$ 2. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \cos\left(-2 + \frac{2i}{n}\right)^2 \frac{8i^2}{n^3}$

D. Compute the following derivatives.

1. $\frac{d}{dx} \int_0^{x^2} e^{t^2} \, dt$ 2. $\frac{d}{dx} \int_0^1 \cos(3t + 4) \, dt$ 3. $\frac{d}{dx} \int_{\sin(x)}^{2x} t^3 \ln(4t^2 - 5) \, dt$

E. Compute the following indefinite integrals

1. $\int 3x^2 \ln(x^2) \, dx$ 9. $\int \frac{1}{1 + 4x^2} \, dx$ 16. $\int \sin(x) \cos(x) \, dx$ 24. $\int \frac{2x + 4}{x^3 - 2x^2} \, dx$
2. $\int x\sqrt{x+1} \, dx$ 10. $\int \frac{\ln(x)}{x} \, dx$ 17. $\int \arcsin(x)^2 \, dx$ 25. $\int \arctan\left(\frac{1}{x}\right) \, dx$
3. $\int \frac{e^{2x}}{1 + e^{2x}} \, dx$ 11. $\int \ln(x) \, dx$ 18. $\int \sqrt{3 + 4x^2} \, dx$ 26. $\int \frac{1}{x^2 - 7x + 99} \, dx$
4. $\int \cos^2(x) \sin^2(x) \, dx$ 12. $\int \frac{1}{x\sqrt{\ln(x)}} \, dx$ 19. $\int x^3 \sqrt{5 - x^2} \, dx$ 27. $\int \left(\frac{1}{x+2} + e^{-x}\right) \, dx$
5. $\int \cos^3(x) \sin^2(x) \, dx$ 13. $\int \frac{\sin(\sqrt{x})}{\sqrt{x}} \, dx$ 20. $\int \frac{x^2 + 2x + 3}{(x-1)(x+1)^2} \, dx$ 28. $\int \cos^2(x) \, dx$
6. $\int x^3 \ln(x) \, dx$ 14. $\int \frac{1}{x^2 + 5x + 6} \, dx$ 21. $\int x^2 \sin(2x) \, dx$ 29. $\int \frac{x^2}{(x^3 + 1)^2} \, dx$
7. $\int \frac{1}{x^2 - 3x} \, dx$ 15. $\int \sin(x)e^x \, dx$ 22. $\int \frac{2x^2 - 1}{(4x - 1)(x^2 + 1)} \, dx$ 30. $\int \frac{2x - 8}{(x^2 + 4)(x + 1)} \, dx$
8. $\int \sec^2(2x) \, dx$

F. Determine if the following integrals are convergent or divergent. If convergent, find the value; if divergent state why.

1. $\int_0^{\infty} \frac{3}{x^2 + 3x + 2} \, dx$ 3. $\int_{-\infty}^{\infty} \frac{dx}{4 + x^2}$ 5. $\int_0^{\pi^2} \frac{\sin(\sqrt{x})}{\sqrt{x}} \, dx$ 7. $\int_0^{\infty} e^{-3x} \, dx$
2. $\int_0^2 \frac{dx}{\sqrt{4 - x^2}}$ 4. $\int_0^2 \frac{dx}{(x-1)^2}$ 6. $\int_0^{\infty} \frac{1}{1 + x^2} \, dx$ 8. $\int_0^3 \frac{e^x}{e^x - 1} \, dx$